

# Stellar Midterm Review Topics

## Equations to memorize

$$F = \frac{L}{4\pi d^2} \quad (1)$$

$$d = \frac{1}{p[{}'']} \text{ pc} \quad (2)$$

$$L = L_{\odot} \left( \frac{M}{M_{\odot}} \right)^{\alpha} \quad (\alpha \simeq 4) \quad (3)$$

$$m_1 - m_0 = -2.5 \log_{10}(F_1/F_0) \quad (4)$$

$$\frac{F_1}{F_0} = 10^{0.4(m_0 - m_1)} \quad (5)$$

$$M_1 - M_0 = -2.5 \log_{10}(L_1/L_0) \quad (6)$$

$$\frac{L_1}{L_0} = 10^{0.4(M_0 - M_1)} \quad (7)$$

$$m - M = 5 \log d - 5 \quad (8)$$

$$\lambda_{\max} = \frac{0.2898}{T(\text{K})} \text{ cm} \quad (9)$$

$$L = A\sigma T^4 \quad (10)$$

$$\tau_{\nu} = \int \kappa_{\nu} \rho ds \quad (11)$$

$$\frac{dP}{dr} = -G \frac{M_r \rho(r)}{r^2} = -\rho g \quad (12)$$

$$\frac{dM_r}{dr} = 4\pi r^2 \rho(r) \quad (13)$$

$$\tau_{ff} \propto (G\rho)^{-1/2} \quad (14)$$

$$\lambda = \frac{1}{n\sigma}, \quad (15)$$

$$t \simeq \frac{1}{n\sigma\nu}, \quad (16)$$

$$\Omega = \alpha \frac{GM^2}{R}. \quad (17)$$

$$P = nkT. \quad (18)$$

$$P_{\text{rad}} = 1/3\sigma T^4. \quad (19)$$

$$P = K_a \rho^{(\phi+1)/\phi} = K_a \rho^{\gamma_a}, \quad (20)$$

$$\kappa = \kappa_0 \rho^a T^b, \quad (21)$$

## Equations I would give you

$$B_{\nu} = \frac{2h\nu^3}{c^2} \frac{1}{e^{h\nu/kT} - 1} \quad (22)$$

$$B_{\lambda} = \frac{2hc^2}{\lambda^5} \frac{1}{e^{hc/\lambda kT} - 1} \quad (23)$$

$$f(\nu) = \sqrt{\left(\frac{m}{2\pi kT}\right)^3} 4\pi\nu^2 e^{-\frac{mv^2}{2kT}} \quad (24)$$

$$\frac{n_i}{n_j} = \frac{g_i}{g_j} e^{-E_{ij}/kT_{\text{ex}}} \quad (25)$$

$$\frac{n_{i+1} n_e}{n_i} \simeq 2 \left( \frac{2\pi m_e kT}{h^2} \right)^{3/2} \frac{g_{i+1}}{g_i} \exp \left[ -\frac{\Phi_r}{kT} \right] \quad (26)$$

$$\frac{dL_r}{dr} = 4\pi r^2 \rho \epsilon \quad (27)$$

$$\frac{dT}{dr}_{\text{rad}} = -\frac{3}{4ac} \frac{\bar{\kappa} \rho}{T^3} \frac{L_r}{4\pi r^2} \quad (28)$$

$$P_{e,\text{deg}} = K'_1 \left( \frac{\rho}{\mu_e} \right)^{5/3}, \quad (29)$$

$$P_{e,\text{deg}} = K'_2 \left( \frac{\rho}{\mu_e} \right)^{4/3}, \quad (30)$$

## **Units**

Parallax

Apparent and absolute magnitudes

## **Stars**

Ranges for physical properties

Spectral types

Lifetimes

H-R diagram

## **Blackbodies**

Planck function

Colors, temperatures, and blackbodies

## **Stellar Equations**

LTE

Mass conservation

Hydrostatic equilibrium

The Virial Theorem

Gravitational Potential

Timescales

## **Gas Physics**

Equations of state

The pressure integral

Various pressures and when they are applicable

Ionization state (Saha)

Electronic state (Boltzmann)

The adiabatic exponent

Opacity

The temperature gradient

## **Fusion**

Computing reaction rates

Proton-proton, CNO, triple alpha, with temperature scalings

r- and s-processes

## **Radiative Transfer**

The equation of radiative transfer and its solutions

The linear absorption coefficient, emission coefficient, and optical depth

Kirchoff's Laws

Line broadening

Equivalent width